

1. Report your test on the claim that the model $y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 + \epsilon$ provides a good fit to x_1, x_2, x_3 and y stored in 4-19data.txt. Use SAS so the correctness of your computation for SSPE and its DF in HW08 can be confirmed.

$$H_0 : \mu(x_1, x_2, x_3) = \beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3$$

versus $H_a : \mu(x_1, x_2, x_3) \neq \beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3$

Test statistic: $F = \frac{MSLF}{MSPE}$

p -value: $P(F(4 - 1, 25 - 4) > F_{ob})$

$$F_{ob} = \frac{299.50199}{25.36667} = 11.81$$

$$p\text{-value: } P(F(5, 20) > 11.81) = 0.0085$$

Reject H_0 . Data do not support that claim of a good fit.

2. Suppose

$SSE(\emptyset)$	=	249657
$SSE(\beta_0)$	=	1857
$SSE(\beta_1)$	=	798
$SSE(\beta_2)$	=	107.8
$SSE(\beta_0, \beta_1)$	=	78
$SSE(\beta_0, \beta_2)$	=	107.7
$SSE(\beta_1, \beta_2)$	=	79
$SSE(\beta_0, \beta_1, \beta_2)$	=	43

- (1) For model $y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \epsilon$, fill out Type I and Type II SS.

	Type I SS	Type II SS
Intercept	$249657 - 1857 = 247800$	$79 - 43 = 36$
X1	$1867 - 78 = 1779$	$107.7 - 43 = 64.7$
X2	$78 - 43 = 35$	$78 - 43 = 35$

- (2) For model $y = \beta_1x_1 + \beta_2x_2 + \epsilon$, fill out Type I and Type II SS.

	Type I SS	Type II SS
X1	$249657 - 798 = 248859$	$107.8 - 79 = 28.8$
X2	$798 - 79 = 719$	$798 - 79 = 719$

3. Based on $n = 25$ observations, $\bar{y} = 22.4$ and $CSS(y) = \sum_i(y_i - \bar{y})^2 = 5785$. In model

	Type I SS
Intercept	12526
x1	5382
x2	168

ANOVA table

Source	DF	SS	MS	F
Model	1	5382	5382	307
Error	23	403	17.5217	
C.Total	24	5785		

DF of SSTO = $n - 1 = 24$; DF of SSE = $n - 2 = 23$; DF of SSM = 1

SSTO = $Syy = 5785$ SSE = $SSTO - SSI_1 = 403$ SSM = $SSTO - SSE = 5382$

or SSM = $SSI_1 = 5382$ SSE = $SSTO - SSM = 403$