

1. For  $A' = A \in R^{n \times n}$  and  $B' = B \in R^{n \times n}$  prove the following two statements

(1) If  $A \geq 0$ , then  $TAT' \geq 0$  for all  $T \in R^{m \times n}$ .

Hint: Give the definition for  $A \geq 0$  first.

(2) If  $A \geq B$ , then  $TAT' \geq TBT'$  for all  $T \in R^{m \times n}$ .

Hint: Give the definition of  $A \geq B$  first.

2. Prove the following statements

(1) If  $\hat{\eta}$  is a LUE for  $\eta$ , then  $A\hat{\eta}$  is a LUE for  $A\eta$ .

(2) If  $\hat{\eta}$  is a BLUE for  $\eta$  and  $B$  is non-singular, then  $B\hat{\eta}$  is a BLUE for  $B\eta$ .