

With data in 5.11 on page 263 from  $N(\mu, \Sigma)$ , SAS produced  $n = 9$ ,  $\bar{X} = \begin{pmatrix} 5.18556 \\ 16.0700 \end{pmatrix}$  and

$$S = \begin{pmatrix} 176.0042 & 287.2412 \\ 287.2412 & 527.8493 \end{pmatrix}.$$

- (1) Construct a 90% confidence region for  $\mu = \begin{pmatrix} \mu_1 \\ \mu_2 \end{pmatrix}$  in the form  $(\mu - b)'A(\mu - b) \leq 1$ . Keep 4 digits after decimal points. Caution:  $A$  but not  $A^{-1}$ .
- (2) Find a 90% confidence interval for  $\mu_1 - \mu_2$ .
- (3) Find simultaneous confidence intervals for  $\mu_1$  and  $\mu_2$  with overall confidence coefficient 90% by Bonferroni method.
- (4) Find simultaneous confidence intervals for  $\mu_1$  and  $\mu_2$  with overall confidence coefficient 90% by Scheffe method.